



According to my understanding, static optimization uses the known kinematics of the model to find a set of muscle activations that satisfy this equation:

$$\sum_{m=1}^n a_m f(F_m^0, l_m, v_m) = \tau_j$$

While minimizing the cost function:

$$J = \sum_{m=1}^n (a_m)^p$$

Where  $l_m$  and  $v_m$  are length and contraction velocity of muscle **contractile element** (CE) respectively. These parameters are different from musculotendon length and contraction velocity.

In the first equation,  $\tau_i$  is known from inverse dynamics. We have three sets of unknowns at each time step including muscle activations, muscle lengths ( $L^M$  in the picture) and muscle fiber velocities ( $\dot{L}^M$ ). We know the total musculotendon length ( $L^{MT}$  in the picture) and velocity from kinematics of the linkage. I was wondering how can we estimate  $l_m$  and  $v_m$  from the kinematics data?